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Suppression of Ground Borne Vibration Induced by High-Speed Lines

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Abstract. Vibration of high-speed lines leads to annoyance of public and lowering real estate values near the railway lines. This hinders the development of railway infrastructures in urbanised areas. This paper investigates the vibration response of an isolated rail embankment system and modifies the component to better attenuate ground vibration. Mainly velocity response is used to compare the responses and the applied force is of 20 kN at excitation frequencies of 5.6 Hz and 8.3 Hz. Focus was made on ground-borne vibration and between the frequency range of 0 and 250 Hz. 3D Numerical model was made using SolidWork software and frequency response was produced using Harmonic Analysis module from ANSYS Workbench software. For analytical modelling MATLAB was used along with Simulink to verify the mathematical model. This paper also compares the vibration velocity decibels (VdB) of analytical two-degree of freedom model mathematical model with literature data. Harmonic excitation is used on the track to simulate the moving load of train. The results showed that modified analytical model gives the velocity response of 75 VdB at the maximum peak. Changes brought to the mass and spacing of the sleeper and to the thickness and the corresponding stiffness for the ballast does not result in significant vibration response. Limitations of two-degree analytical model is suspected to be the cause of this inactivity. But resonance vibration can be reduced with the aid of damping coefficient of rail pad. Statistical analysis methods t-test and ANOVA single factor test was used verify the values with 95% confidence.

Keywords: Vibration, Rail, Embankments, Analytical model, Numerical model.

1 Introduction

Rail transportation was a novel mode of transportation created during the enlightened era of industrial revolution in 18th century [1]. Back then, the trains were driven by coal powered steam engines which were loud, dirty and puffed out nauseating thick black smoke. Nevertheless, this mode of transportation was popular among people because, compared to

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available alternative modes of transportation, trains had many appealing benefits. These include regular intervals of travelling to a predetermined location safely and cheaply. The benefits have increased over the years with technological advancement in engines which has allowed it to travel much faster and efficiently with cleaner and more powerful diesel engines

This popularity has been retained, despite remarkable advances in automobile technology in recent years. Moreover, train usage is raising in urbanised areas across the world for both developed and developing countries. Abe *et al.* [2] investigated rail travel demand in Tokyo from 1950 to 2010 and found that the usage was still increasing, with more travellers using underground trains nowadays. Also, a study made on the market competition of the European rail freight trains, which are large cargo trains, by Laroche *et al.* [3] similarly found that the market was growing despite high initial start-up cost in European Union countries. Furthermore, Chen *et al.* [4] stated that since the beginning of 2000, Chinese government has started to build a massive rail system infrastructure and the effects of this decision has been beneficial to the economy and livelihood.

Therefore, rail travel is still a booming and essential industry for developed countries and even greater for developing countries. But despite the advances in technology, the current railways still have many issues. The most recognisable problems with the railway are vibration and noise. This paper will focus on the ground-borne vibrations which are caused by the movement of the wheel on the track, which propagates vibration from the track to the surrounding areas. These vibrations can be an annoyance to humans who live in nearby buildings. This becomes more problematic in urbanised cities, as Connolly *et al.* [5] states that, the economical repercussion due to high vibrations in city areas are more serious as these vibrations can reduce real estate values and can entirely disrupt the work in sensitive workplaces such as record studios, tv studios and theatres. The paper states that even though these sensitive buildings are fewer compared to residential buildings, the high number of reported complaints from these places shows that there is a direct detriment to the working condition of these places due to railway lines. It also cites that ground vibration is also a growing concern in most European countries due to increasing railway lines and soaring frequency of trips per day.

This research investigates and proposes a modified track embankment to suppress the vibrations. To achieve that the components of the embankment needs to be investigated and the influence of the parameters on the vibration needs to be identified through literature review. Referring to the parameters influence on vibration, the components will be modified to form a mathematical model. Analytical calculations using this model will be conducted using MATLAB and numerical calculations using Finite Element analysis will be made using ANSYS software. The analytical and numerical calculations are compared with each other and also verified using literature data.

1.1 Objectives

Vibration induced by high speed train is a growing urban issue and mitigating methods needs to be put in place to attenuate the vibrations. Generally, the methods to lower the effects of vibration can be classified into two, which is active mitigation, where modification is applied to the railway support and passive mitigation, where nearby buildings are modified with better vibration damping properties. This paper focuses on active mitigation as this is the most sought out method in real life [4].

To modify the railway support or embankment, the properties of the components which makes up the railway embankment is investigated. Next the properties are altered and the result of that quantified using the research methods of analytical and numerical modelling.

1. Investigate the parameters which influence ground vibration induced by high speed lines.
2. To modify the embankment components parameters to achieve greater vibration suppression.
3. To verify the accuracy of the analytical and numerical modelling with each other and literature data.

1.2 Literature review

1.2.1 Railway components

A typical rail embankment has basic four components, track, sleeper, rail pad and ballast, as shown in Figure 1. In addition to these four, external dampers are used in some railways as well. The track is the steel bar on which the train travels and the sleepers are orderly arranged blocks of concrete blocks on which the track is placed. Ballast is the floor which is made from small stones on which the sleeper is placed and half buried in. The rail pad is the placed on the sleeper and acts as the contact to the track. Dampers are external damping structures placed on the track and sleeper to absorb vibrations. The three components to which the parameter changes are made are sleepers, ballast and dampers.

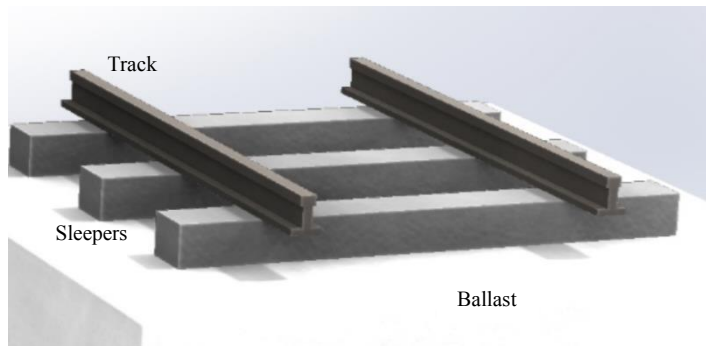


Fig. 1. Rail, sleeper and ballast of a railway embankment.

1.2.2 Types of Vibration

Vibration is a periodically repeating motion. When a train moves on a rail embankment, different types of vibrations occurs. Abe *et al.* [6] states that the main causes for vibration is due to the roughness between the track and the wheel and due to differing stiffness due to periodically placed sleepers. A vibration caused by this sleeper placement is called the pinned-pinned resonance and it occurs when the vibration wavelength is same as the sleeper spacing [7]. Static loading on the track also causes vibration and in Auresh *et al* [8] it is modelled as a quasi-static load as the load is moved along the track. But it is the wheel/track irregularities which causes most significant vibrations. Nielsen *et al.* [9], investigates the effect on the track as the wheel becomes more flattened due to skidding and grinding. The results showed that the level of ground vibration was much higher for trains with flattened wheels.

1.2.3 Selected parameters

For sleeper, the parameters selected are spacing between sleepers and its mass. Abe *et al.* [6] states that by reducing the spacing the pinned-pinned vibration can be reduced. It also a study by Dwight *et al.* [10] found that mass of the sleeper effects the wave frequencies of the track. The dimension of the sleeper is also investigated because changing the height decreases the bending movement as stated by Kollo *et al.* [11] and this could influence the vibration as well.

Thickness and stiffness is selected for the ballast as these two parameters can be easily altered by increasing the height by adding more stones and by changing the stiffness by altering the size of the stone. Benedetto *et al.* [12] investigated the response of a rubber mixed ballast which would have low stiffness and the results should increase in vibration in low frequency bands of 10 - 30 Hz. Zhang *et al.* [13] found that the increase in thickness, decreases particle velocity. This would decrease the vibration levels as well.

The influence of rail pad on the vibration and flexural modes of the sleeper was investigated by Kaewunruen *et al.* [14] with results showing a relation between the rail pad stiffness and the bending mode with generally high stiffness of rail pad, reducing translation and rotational modes. Results also showed that most damage occurs to the sleepers in the resonant frequencies due to the modes of vibration. It is also cited in Abe *et al.* [6] that the stiffness reduction of the rail pads can influence a lower vibration on the rail system. This component is a focus of this paper due to the ease of adjustability. Changing the rail pad is economically viable compared to changing larger components such as track, sleeper and ballast. Furthermore stiffness and damping are the only variable parameter available for this component since changes to the dimension and mass are limited by the track and sleeper dimensions.

2 Modelling Methodology

2.1 One-dimensional Analytical model and Harmonic excitation

The literature review showed that the type of model used for study reflected the objectives of that study. For example, Zhang *et al.* [15] used two-dimensional analytical model as the effect of one unsupported sleeper on the other sleeper is required to be known. For investigation into wheel and track interactions as in the case of Ferrara *et al.* [16] where a new numerical model to simulate the wheel/track irregularity vibrations is presented and in the case of Nielsen *et al.* [9] where the vibration and the force impacts caused by damaged wheels are investigated, a non-linear Hertzian theory is used would also mean a two-dimensional calculation. As for Dwight *et al.* [10] which compares the Timoshenko continuous beam theory with semi-analytical finite element (SAFE) calculations uses three-dimensional modelling as the lateral in addition to vertical movement of the beam is investigated.

To comply with the objectives of this study, the model uses a one-dimensional model as the effects of direct harmonic load is investigated. Harmonic forces are useful for the investigation as they are continuously applied forces which stimulates the effects of a moving wheel and the consequent stiffness variation in addition to allowing easier understanding of resonances or parametric excitations which provides the maximum values [8]. These extremes are useful to gauge the effectiveness of parameter changes.

Therefore, for this study series of increasing degrees of freedom models up to three degrees of freedom are formed using spring, mass and damping blocks. Only one side of the rail track is used, hence the mass of the ballast and sleeper and excitation force are halved. Further changes to the model are made based on the properties of the components.

2.2 Properties of Embankment Components

The important three components are the mass, damping and stiffness of the components. While mass is an easy property to determine, stiffness and damping are more challenging. Damping of materials is very difficult to discern unless by experimentation [18] and while the stiffness of a component might be simpler in comparison, stiffness changes with the dimension of the component. This is challenging for the ballast where a small volume is required to be isolated to study the effects of vibration. The effort was simplified with the analytical data from Ferrara *et al.* [16] and Zhai *et al.* [19]. Table 1 shows the properties of different components. The data is taken from sources which has similarity to parameters which is studied in this research. This includes high-speed trains at least 100 km/s of speed, concrete sleeper and at-grade railways (not underground subways or LRTs).

To calculate the stiffness the ground directly below the sleeper is taken in to account in a diverging geometry similar to a trapezoid [19]. This geometry takes in account of the load distribution. Stiffness is calculated by the formula provided by Ferrara *et al.* [16].

$$k = \frac{2(l - b) \tan \phi}{\ln \left[\frac{l(2h \times \tan \phi + b)}{b(2h \times \tan \phi + l)} \right]} \times E$$

(1)

Table 1. Data for the components.

| Component | Property | Value | Units |
|------------|-----------------------|-------------------------------|-------------------|
| Rail track | Mass | 51 | kg/m |
| | Length | 850 | Mm |
| | Young Modulus | 207 [16] | GPa |
| Rail pad | Stiffness | 20 – 3500 [14] | MN/n |
| | Damping coefficient | 15 [9], 20 [14] 75 [19] | Ns/m |
| | Size | 148 × 180 × 10 [20] | Mm |
| Sleeper | Mass (half) | 150 [21, 19] | Kg |
| | Spacing | 600 [6, 10] | Mm |
| | Dimension | 1250 × 250 × 200 [8] | Mm |
| | Poisson Ratio | 0.15 [8] | |
| | Density | 2500 [8], 2750 [15] | kg/m ³ |
| Ballast | Stiffness | 280.4 | MN/m |
| | Damping coefficient | 132 [9], 165 [15] 58.8 [19], | kNs/m |
| | Modulus of Elasticity | 0.11 [19] | GPa |
| | Thickness | 300* (200 mm subballast) [21] | Mm |
| | Angle | 35 [19] | Degree |

2.3 Properties of Embankment Components

The excitation force is the axle load placed on the track from the wheels of the train. This force is not the weight or the static load of the train itself, but the downward force on the track due to the movement of train. In fact, axle load of a train changes with the speed of the train [8]. Similarly, to the embankment properties, the axial force should also match with the experimental excitation. The type of train from which the measurements were taken by Connolly *et al.* [21] is a high-speed TGV *Reseau* (TGV), train which operates at an average speed of 294.7 km/h or 81.89 m/s. The axle load on the track only increases up to a certain speed and from then onwards the axial load decreases [8]. Therefore, fast trains such as Sweden's X2000 train which operates at 200 km/h [22] had a lower axial load of 18.25 kN than Spain's Talgo train which operates at 160 km/h [23] had a maximum axle load of 75 kN. As the axial load of TGV was not provide, an axle load of 20 kN is selected as this value is closer to the axle load of X2000.

The excitation frequency is selected to be 5.6 Hz and 8.3 Hz for speed of 200 km/h and 300 km/h respectively. This is for an axle distance of 10 m.

2.4 Analytical model using One, Two and Three Degrees of Freedom

The equation of motion for a single degree mass with damping and stiffness is given by Equation 2 and the harmonic excitation by Equation 3. [24]

$$m_T \ddot{x} + c_{eq} \dot{x} + k_{eq} x = 0 \quad (2)$$

$$F \cos(\omega t) \quad (3)$$

Where, m_T is the mass. \ddot{x} is the acceleration. c_{eq} is the equivalent damping of the system. \dot{x} is the velocity. k_{eq} is the equivalent stiffness of the system and x is the displacement. For the Eq. 2 the force is represented by F and ω is the driving frequency and t is time.

The amplitude of the steady force response is given by the Equation 4 and the phase, φ is given by the Equation 5.

$$X = \frac{F}{\sqrt{[(k_{eq} - m_T \omega^2)^2 + (c_{eq} \omega)^2]}} \quad (4)$$

$$\varphi = \tan^{-1} \left(\frac{2\pi \omega_T \omega}{\omega_T^2 - \omega} \right) \quad (5)$$

Where, π is the damping ratio.

The Equations 4 and 5 are used to find the harmonic response of the system. Equation 6 shows the final form of the equation. The homogenous or transient response is not included as the motion begins from zero initial velocity and displacement, therefore these responses will be zero.

$$x(t) = X \sin(\omega t - \varphi) \quad (6)$$

The analytical model is also verified using MATLAB Simulink model shown in Figure 2. The results from Equation 6 is verified by the Simulink model which is a second order model calculated using ordinary differential equation of Dormand-Prince method.

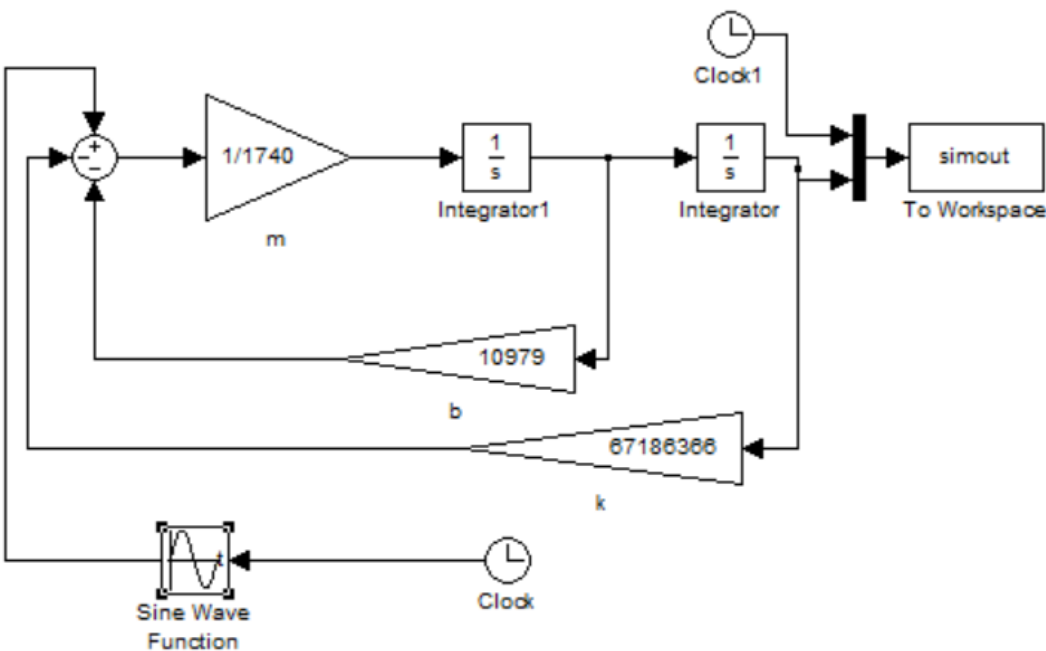


Fig. 2. Simulink model for harmonic excitation for a spring damper system.

Multi-degree of freedom models is more complicated than one degree of freedom as each mass are coupled with the subsequent masses. Therefore, decoupling is required to measure the individual response of the mass. Equations 7 and 8 shows that general two-degree and three-degree of freedom system under harmonic force.

$$\begin{bmatrix} m_1 & 0 \\ 0 & m_2 \end{bmatrix} \begin{Bmatrix} \ddot{x}_1 \\ \ddot{x}_2 \end{Bmatrix} + \begin{bmatrix} c_1 + c_2 & -c_2 \\ -c_2 & c_2 \end{bmatrix} \begin{Bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{Bmatrix} + \begin{bmatrix} k_1 + k_2 & -k_2 \\ -k_2 & k_2 \end{bmatrix} \begin{Bmatrix} x_1 \\ x_2 \end{Bmatrix} = \begin{Bmatrix} 1 \\ 0 \end{Bmatrix} F e^{i\omega t}$$
(7)

$$\begin{bmatrix} m_1 & 0 & 0 \\ 0 & m_2 & 0 \\ 0 & 0 & m_3 \end{bmatrix} \begin{Bmatrix} \ddot{x}_1 \\ \ddot{x}_2 \\ \ddot{x}_3 \end{Bmatrix} + \begin{bmatrix} c_1 + c_2 & -c_2 & 0 \\ -c_2 & c_2 + c_3 & -c_3 \\ 0 & -c_3 & c_3 \end{bmatrix} \begin{Bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \end{Bmatrix} + \begin{bmatrix} k_1 + k_2 & -k_2 & 0 \\ -k_2 & k_2 + k_3 & -k_3 \\ 0 & -k_3 & k_3 \end{bmatrix} \begin{Bmatrix} x_1 \\ x_2 \\ x_3 \end{Bmatrix} = \begin{Bmatrix} 1 \\ 0 \\ 0 \end{Bmatrix} F \cos \omega t$$
(8)

Beginning from three-degree of freedom, Equation 8 shows the general system of Figure 3. The masses from top to bottom with the subscript 1,2 and 3 are of track, sleeper and ballast. The stiffness and damping coefficient of subscript 1 are of the rail pad, then for the ballast for subscript 2 and 3. As the force is applied on the track, only the first matrix for force is placed by a harmonic excitation while the rest are zero.

For the two-degree of freedom, in Equation 7 the mass (m_1) combines the mass of track and the sleeper. Also stiffness and the damping are for the rail pad and for ballast. The property of ballast is not duplicated as in the three-degree of freedom equation.

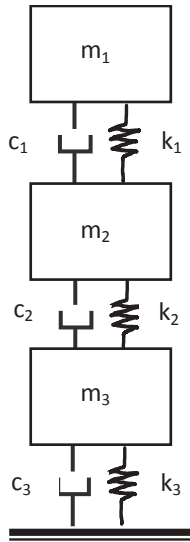


Fig. 3. Three degree of freedom system.

Two separate methods have been used for solving the Equations 7 and 8. For two-degree of freedom system, mechanical impedance $Z(i\omega)$ is used to find the response for the two-degree of freedom displacement, velocity and acceleration as shown in Equations 9 – 13.

$$x_1(t) = X_1 e^{i\omega t} \tag{9}$$

$$x_2(t) = X_2 e^{i\omega t} \tag{10}$$

Equations 9 and 10 are steady state displacement solution for the amplitudes X_1 and X_2 with the forcing frequency of ω . The values for the amplitudes are obtained from the mechanical impedance Equations 12 and 13.

$$Z_{rs}(i\omega) = -\omega^2 m_{rs} + i\omega c_{rs} + k_{rs} \tag{11}$$

The subscript rs corresponds to the location of the property in the matrices in Equation 7.

$$X_1 = \frac{z_{22}(i\omega) F_{10}}{z_{11}(i\omega) z_{22}(i\omega) - z_{12}^2(i\omega)} \tag{12}$$

$$X_2 = \frac{-z_{12}(i\omega) F_{10}}{z_{11}(i\omega) z_{22}(i\omega) - z_{12}^2(i\omega)} \tag{13}$$

But substituting the values of X_1 and X_2 to Equations 9 and 10, the displacement due to force can be calculated. To find the velocity and the acceleration the Equations 9 and 10 are differentiated once for velocity and twice for acceleration.

An easier route has been taken for three-degree of freedom equation by using MATLAB ordinary differential equation 23 for calculation. Appendix A shows the differential equations used where the three equations from the matrix in Equation 8 is set as six first order differential equations.

Another important formula for quantifying the level of vibration is decibels formula Equation 14. Decibels helps to standardise results so that it can be compared with data from other sources [25].

$$L_v = 20 \log_{10} \left(\frac{v}{v_{ref}} \right) \tag{14}$$

L_v is the velocity level represented in decibels and v_{ref} is the reference velocity. This velocity is an accepted value for reference agencies such as International Organisation for Standardisation (ISO) and Federal Transit Administration (FTA). The value used in this paper is $2.54 \times 10^{-8} m/s$ which is the value used by the FTA [25].

2.5 Numerical modelling

Similar to the analytical model, the numerical model uses a single track, sleeper and ballast is shown in Figure 4. But in addition to the analytical modelling a rail pad is modelled and placed as well. Furthermore, the ballast was modelled in a trapezoid geometry for model A and model B uses two sleepers to test the response due to varying the sleeper distance. The components were modelled from SOLIDWORK and was imported to ANSYS Workbench. The bodies were given the material properties and then Harmonic Response module was selected to apply a force of 10000N on the track surface. The boundary condition is set as frictionless support and the frequency range is selected from 0 to 250 Hz with 10 Hz increment. Same properties from Table 1 is used for the material data.

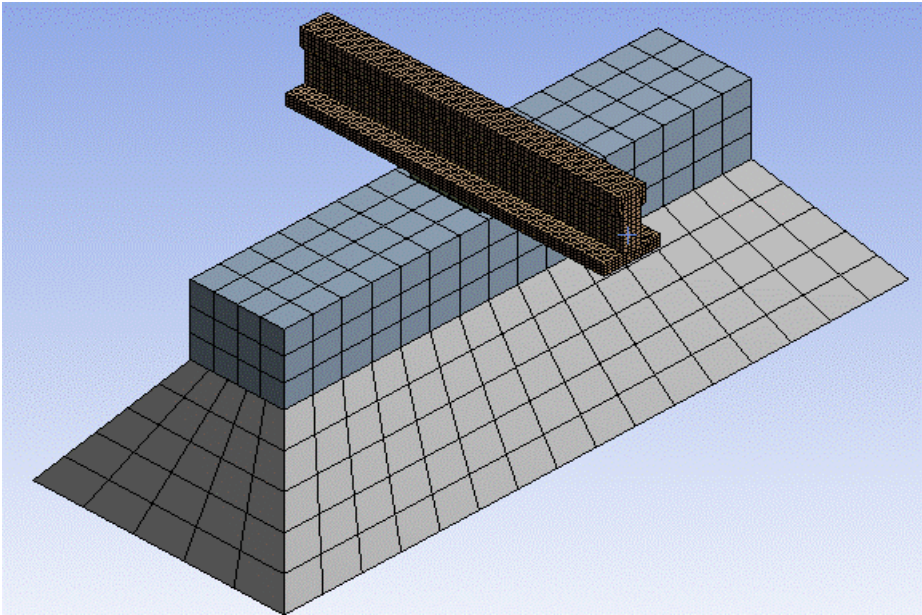


Fig. 4. One sleeper model A.

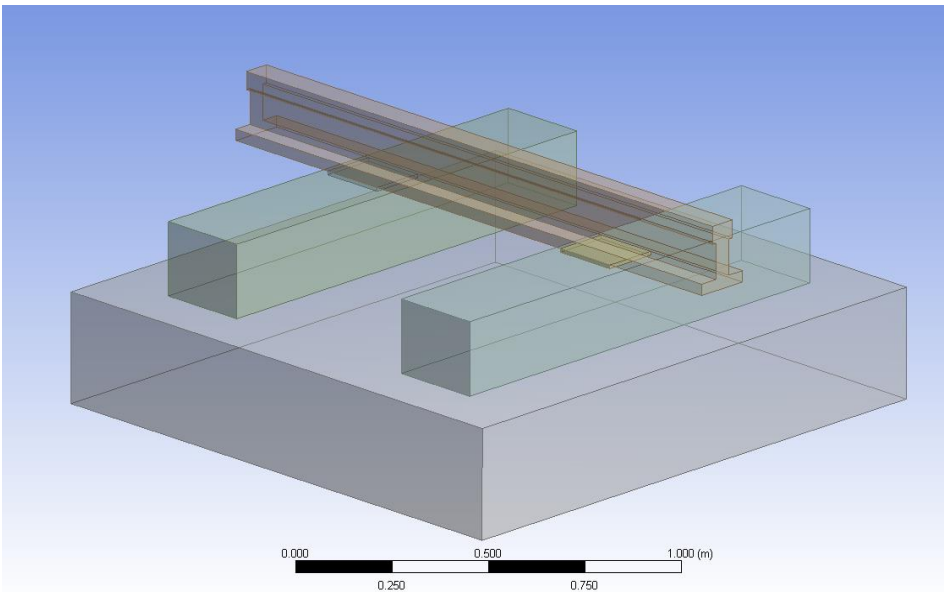


Fig. 5. Numerical model of the track, sleeper and ballast with the force being applied to the track in negative y-direction.

Table 2. Mesh Property of Model A and B

| Mesh Property | Model A, one sleeper | Model B, two sleepers |
|--------------------|--|--|
| Element size | For track 0.01 m Rest of the body Automatic | For track 0.01 m Rest of the body Automatic |
| Meshing Method | Hexagonal | Hexagonal |
| Number of Elements | 61714 | 1339267 |
| Element Quality | 0.955 | 0.962 |
| Skewness | 0.0574 | 0.0486 |

3 Results and Discussion of Analytical and Numerical Modelling

The analytical model is done using formulas and calculations. Therefore, an error might occur in the calculations which might offset the results. To verify that there is no such error, Simulink model is made to calculate the harmonic motion of a second order differential equation. The results showed that there is observable correlation, and this is statistically proven with the Table 3. Pearson correlation, which indicates strong relation between the two means as the value is close to value one, and the value of the statistical test, 0.9733 is very close to one. Furthermore, the t-critical is much higher than the t-statistical value, hence there is 95% confidence that the mean is similar.

There are many disadvantages of using the one-degree of freedom as the effects of individual components properties cannot be discussed as the total and equivalent values are used. Therefore, the second-degree of freedom model from Equations 9 and 10 are used to provide the results. The results are formed with velocity response for two masses. The first mass is the total mass of track and sleeper and the second mass is that of the ballast. These results are also given in frequency domain as well to compare with the numerical results for harmonic excitation. The three-degree of freedom is not used because second-degree of freedom model is easier to convert to velocity response and the mass of track and sleeper is not large compared to ballast, so they can be combined.

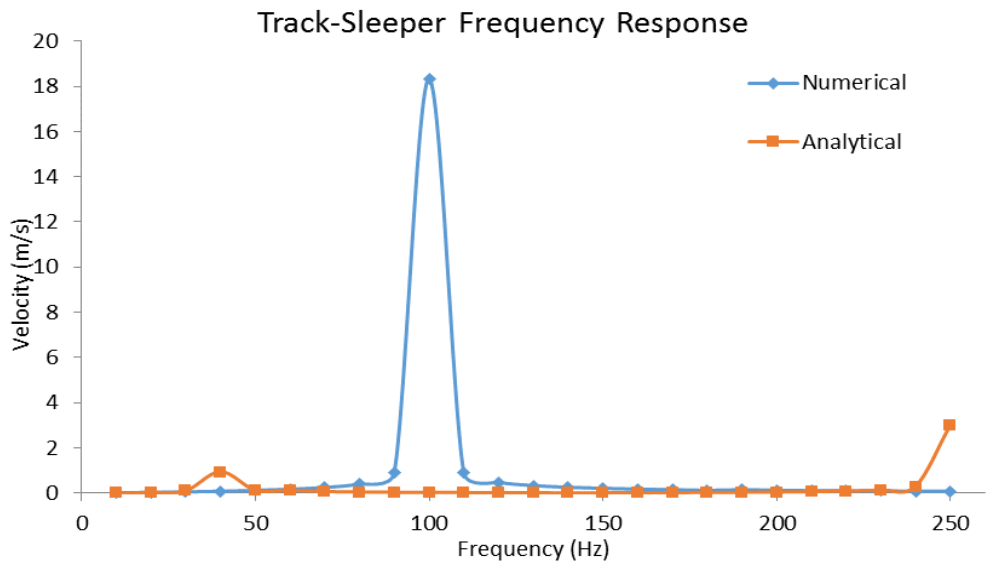


Fig. 6. Velocity frequency of numerical and analytical second-degree freedom model for track-sleeper.

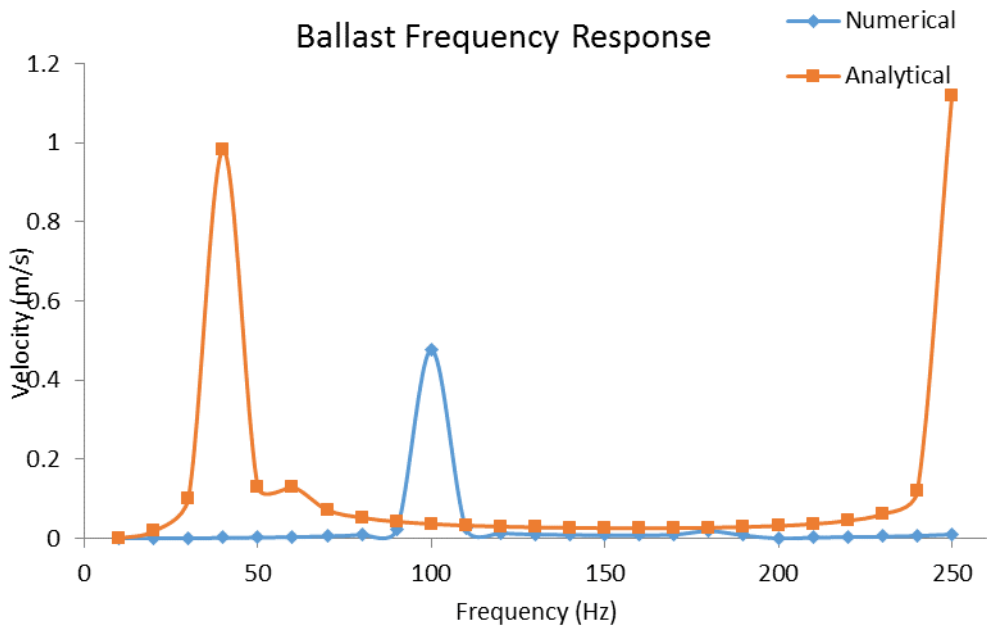


Fig. 7. Velocity frequency of numerical and analytical second-degree freedom model for ballast

While, the visual comparison between the numerical and the analytical model, Figures 6 and 8 might seem apparent because of the peaks, the lower values remain close to each other for both figures. Provides 95% confidence that the means are the same for both of the

models. The t-statistical is lower than the t-critical for both the tests but the Pearson Correlation is low. This means that while correlation is not very high, the means are nevertheless same. The peaks for numerical model is at 100 Hz and for analytical at 40 and 250 Hz. The modal simulation using ANSYS Workbench modal analysis module shows that at 100 Hz the natural frequency of the rail pad is reached as shown in Figure 8. This causes the high vibration response. Therefore, the excitation frequency must not reach this 100 Hz while using the rail pad with this particular stiffness form Table 1 of 20 MN/m.

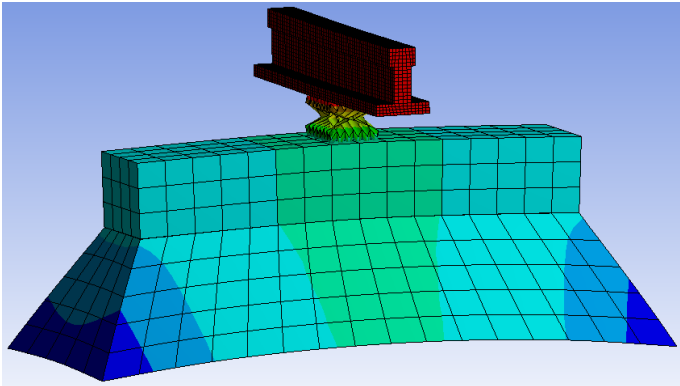


Fig. 8. Modal analysis for numerical Model A using modal analysis

Table 3. Paired Two Sample for Means t-test for Analytical and Simulink results

| | <i>Simulink</i> | <i>Analytical</i> |
|------------------------------|-----------------|-------------------|
| Mean | 1.48E-05 | 7.56E-06 |
| Variance | 1.44E-07 | 1.82E-07 |
| Observations | 21 | 21 |
| Pearson Correlation | <u>0.973328</u> | |
| Hypothesized Mean Difference | 0 | |
| Degree of Freedom | 20 | |
| t Stat | <u>0.317091</u> | |
| P(T<=t) two-tail | 0.754461 | |
| t Critical two-tail | <u>0.686954</u> | |
| Mean | <u>0.973328</u> | |

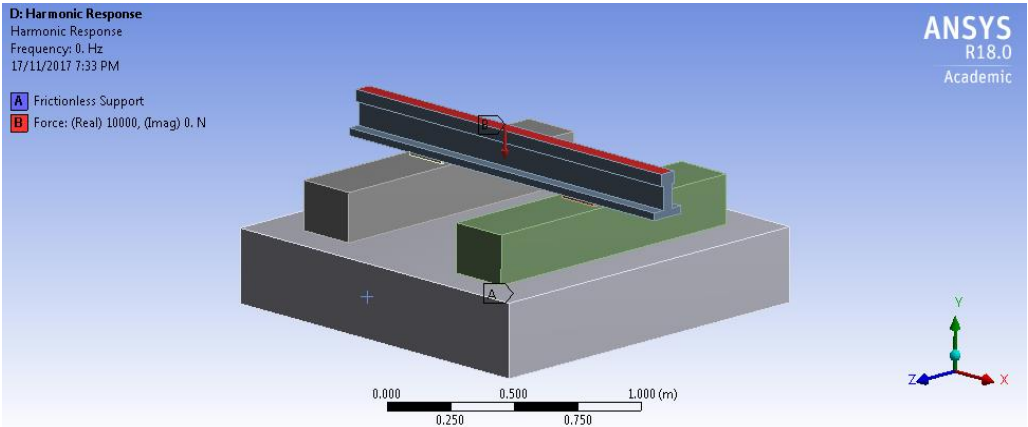


Fig. 9. Model used to study the vibration response to different sleeper spacing

Numerical model to investigate the relation between acceleration response due to sleeper distances of 50, 60 and 70 cm was simulated using the model as shown in Figure 9. The results provided in Appendix B gave insufficient difference to the response. This is validated using ANOVA test in Table 4. where the F-critical 3.12 is greater than F-statistics of 1.88. The reason for using ANOVA is that means of three sets needed to be compared.

Table 4. Show the summary of variance of the sleeper spacing and the F-test

| SUMMARY | | | | | | |
|----------------------------|--------------|------------|----------------|-----------------|----------------|---------------|
| <i>Groups</i> | <i>Count</i> | <i>Sum</i> | <i>Average</i> | <i>Variance</i> | | |
| 50cm | 25 | 14.24983 | 0.569993 | 0.805951 | | |
| 60cm | 25 | 208.6954 | 8.347815 | 578.3901 | | |
| 70cm | 25 | 77.36599 | 3.09464 | 48.01165 | | |
| | | | | | | |
| | | | | | | |
| ANOVA | | | | | | |
| <i>Source of Variation</i> | <i>SS</i> | <i>df</i> | <i>MS</i> | <i>F</i> | <i>P-value</i> | <i>F crit</i> |
| Between Groups | 787.2018 | 2 | 393.6009 | 1.882634 | 0.159604 | 3.123907 |
| Within Groups | 15052.99 | 72 | 209.0692 | | | |
| | | | | | | |
| Total | 15840.19 | 74 | | | | |

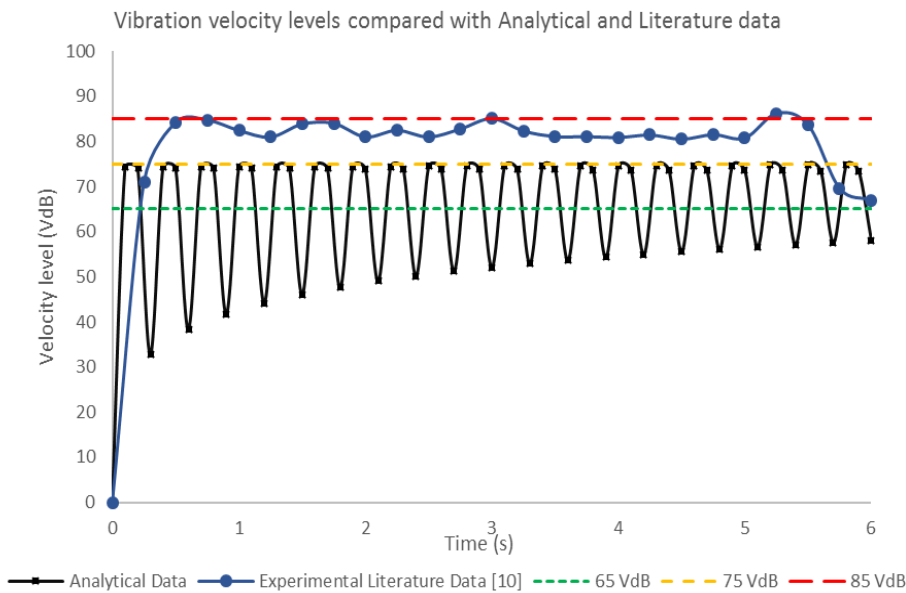


Fig. 10. Actual literature data compared with analytical data with benchmarking of 65 VdB, 75 VdB and 85 VdB

It was found out by analytical calculations that rail pad stiffness produces high response on the vibration of the system. Therefore, using Matlab, the lowest possible value of vibration was produced with the provided pad stiffness from Table 1. The as the stiffness increases the vibration of the system decreased. Therefore, the highest stiffness value of 3500 MN/m value was used. This material corresponds to high density Ethylene vinyl acetate polymer (EVA) [14]. The maximum value from the analytical data was compared for the frequency using alternatively 5.6 and 8.3 Hz. As 8.3 Hz had higher magnitudes it was selected.

The lowest analytical vibration response was then converted to velocity decibels which has the reference value of $2.54 \times 10^{-8} \text{ m/s}$ [25] to make it easier to compare with the benchmark values. In Figure 10, three dashed lines of values 65, 75 and 85 VdB are the three bands of vibration levels which will be felt by humans with the intensity increasing with the values. This is stated in the “Transit Noise and Vibration Impact Assessment”, released by American Federal Transit Administration (FTA) [25], that while 65 VdB is barely precipitable for humans and 75 VdB can be annoying for some, at 85 VdB people will find this level disruptive and is acceptable if only infrequent amount of trips. Changes to the rail pad stiffness is effective for suppressing vibrations which is shown in Figure 10. This statistically proven with ANOVA single factor test of 95% confidence in Table 5 as the F-statistical values of 8.47 larger than 3.95 F-critical. ANOVA single factor was used due to the difference in count for the results.

Table 5. Show the summary of variance of the analytical and literature data and the F-test

| SUMMARY | | | | | | |
|----------------------------|--------------|--------------|----------------|---------------------|----------------|---------------------|
| <i>Groups</i> | <i>Count</i> | <i>Sum</i> | <i>Average</i> | <i>Variance</i> | | |
| Analytical Data | 61 | 3976.86 2 | 65.1944 6 | 211.733 8 | | |
| Literature Data | 29 | 2181.41 2 | 75.2211 2 | 278.957 6 | | |
| ANOVA | | | | | | |
| <i>Source of Variation</i> | <i>SS</i> | <i>Df</i> | <i>MS</i> | <i>F</i> | <i>P-value</i> | <i>F crit</i> |
| Between Groups | 1976.05 | 1 | 1976.05 | <u>8.47641</u> 8 | 0.00455 8 | <u>3.94932</u> 1 |
| Within Groups | 20514.8 4 | 88 | 233.123 2 | | | |
| Total | 22490.8 9 | 89 | | | | |

4 Conclusions

In this study, a simplified analytical model and a numerical model is made to understand the vibration response due to a train load which is simulated by harmonic excitation. The numerical modelling showed that a resonance does occur 100 Hz range which belongs to the rail pad. List of components of the rail embankment has been reviewed using journal articles and their vibration influencing parameters in addition to their other properties have been complied and refined to make sure they meet the scope of the project. Then analytical and numerical models where created using ANSYS and Matlab for numerical and analytical respectively. A model very closed to the actual literature data was made and the vibration was supressed by increasing the rail pad stiffness. Comparison between the modified analytical model gives the velocity response of 75 VdB as the maximum peak.

Two-dimensional modelling is required to investigate more complex vibrations and also take in the influence of geometry of the components such as sleeper spacing. Also scope of the project needs to be more focused on particular train or trains from certain region, as different regions uses different types of trains and embankment. Most importantly an acoustic assessment is required to understand the noise generated under the new rail pad stiffness. If the stiffness had worsened the noise, other methods needs to be explored such as using external dampers.

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